

Sources of Variation

(1)	<p>∃ Variation <u>between</u> group means</p> <p>Attributed to treatment(s) (Treatment variation)</p> <p>(Factor of interest)</p> <p>Regression: $\Sigma(\hat{y} - \bar{y})^2$</p> <p>Anova: $\Sigma n_i(\bar{x}_i - \bar{x})^2; df = (k - 1)$</p> <p style="text-align: center;">SSB=SST-SSE</p>	<p>SS_B (Between)</p> <p>SS_T (Treatment)</p> <p>SS_{model}</p> <p>TSS (tmt SS)</p>
(2)	<p>∃ Variation <u>within</u> any group</p> <p>"Within group" variation</p> <p>Unexplained random error</p> <p>("Residual" variance, or "error" variance)</p> <p>Regression: $\Sigma(y - \hat{y})^2$</p> <p>Anova: $\Sigma(x_i - \bar{x}_i)^2; df = (N - 1) - (k - 1) = N - k$</p>	<p>SS_W (within)</p> <p>SS_{err} (error)</p> <p>SS_{resid}</p> <p>RSS (residual SS)</p>
(3)	<p><u>Total variation</u></p> <p>Lump all observations together, ignoring factors of interest.</p> <p>Deviation from the grand mean</p> <p style="text-align: center;">$\Sigma(x_i - \bar{x})^2; df = (N - 1)$ $df \cdot \text{var}(x_i)$</p> <p>Or calculate from SST=SSB+SSW, or SST=SS_{tmt} + SS_{error}</p> <p>Under H₀, MS_{tmt} ≈ MS_{err} (MSB == MSW) and both estima σ_e^2</p> <p>If H₀ false, MS_{tmt} > MS_{err}.</p> <p>The "residual standard error" is the "root MSE" (i.e., square root of the mean square error)</p> <p>R² is the variation explained by the model = SS_{tmt}/SS_{err}.</p>	<p>SS_{TOT} (total)</p>